

1 of N

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The basic game is to wind a curve through a cubic grid, grouped in eights into larger cubes, grouped by eights into larger cubes, grouped by eights into larger cubes — exactly once entering and exiting each cube of each size.



But up to symmetry, how many such curves are possible? This number is part of the real name of this sculpture. We have left this calculation as a puzzle, and in the meantime, call the sculpture 1 of N.

We made a quick model out of sixtyfour pieces of plumbing.



Moreover, we needed to be able to rummage around the set of all such curves, to try to make some rational choices about the final form of the sculpture.

(Chaim's formalism of "Regular Production Systems" are designed to capture just this sort of non-deterministic production system acting under regular constraints, arising in a wide variety of settings.)



Alas, I cannot find the folder with extensive hand-written notes and diagrams developing the structure.

From these, models were made and code was written.

This first set of wooden tiles consists of eight bricks, and eight clumps of three bricks, in the shape of an L.

It is not difficult to enumerate all arrangements of these, up to symmetry, within a 4x4 cube.







Now we want to begin to enumerate all possible ways to substitute in. We presume that the strings represent closed curves. We first encode all "shifts" at the vertices.	
There are six possible ways to shift a vertex (see notes), which for lack of something simpler we represent as	
vA, vB, vC, vD, vE, vF	
Protect[vA, vB, vC, vD, vE, vF]	
{vA, vB, vC, vD, vE, vF}	
<pre>NextShitCanBe(edgeSymbol_, lastShift_] := Switch(edgeSymbol, 0, Which(HemberQ[(VA,,VA,VE), JastShift], (VA,,VA,), HemberQ[(VG,,VG,,VB, JastShift), (VA,VA), HemberQ[(VG,,VG,VE,JastShift), (VG,VG,VG), True, Print['ERNOR 0"]], 1, Which(HemberQ[(VA,VA,VE,JastShift), (VA,VA,VE), HemberQ[(VA,VA,VE,JastShift), (VA,VA,VE), HemberQ[(VA,VA,VE,JastShift), (VA,VA,VE), HemberQ[(VA,VG,VG,JastShift), (VA,VA,VE), HemberQ[(VA,VG,VG,JastShift), (VA,VA,VE), HemberQ[(VA,VG,VG,JastShift), (VA,VA,VE), HemberQ[(VA,VG,JastShift), (VA,VA,VE), HemberQ[(VA,VG,JASTSHIft), (VA,VA,VE), HemberQ[(VA,VG,JASTSHIft), (VA,VA,VE), HemberQ[(VA,VG,JASTSHIft), (VA,VA,VE), HemberQ[(VA,VG,JASTSHIFT), (VA,VA,VE), HemberQ[(VA,VG,JASTSHIFT), (VA,VA,VE), HemberQ[(VA,VG,JASTSHIFT), (VA,VA,VE), HemberQ[(VA,VG,VG,VG,VG), HASTSHIFT, (VA,VA,VE), HemberQ[(VA,VG,VG), HASTSHIFT, (VA,VA,VE), HemberQ[(VA,VG),VA,VE], HASTSHIFT, (VA,VA,VE), HemberQ[(VA,VA,VE], HASTSHIFT, (VA,VA,VE),</pre>	{{ $vE, 0, vB_1$ }, {1}, { $vB_1, 1, vB_1$ }, {0}, { $vA_1, 3, vA_2$ }, {0}, { $vB_2, 1, vF$ }, {2}, { $vA_1, 0, vF$ }, {1}, { $vC_2, 1, vC_1$ }, {0}, { $vD_2, 3, vE$ }, {0}, { $vB_1, 1, vF$ }, {2}, { $vA_2, 1, vD_2$ }, {3}, { $vD_1, 0, vC_2$ }, {3},
CanonicalSubstitution[str_] := (
ss = {vA ₁ }; sstr = str;	$\{VB_1, 0, VA_2\}, \{1\}, \{VD_2, 0, VC_1\}, \{2\}, \{2\}, \{VB_1, 0, VA_2\}, \{1\}, \{VB_2, 0, VC_1\}, \{2\}, \{2\}, \{1\}, \{2\}, \{1\}, \{2\}, \{1\}, \{2\}, \{1\}, \{2\}, \{2\}, \{1\}, \{2\}, \{1\}, \{2\}, \{1\}, \{2\}, \{1\}, \{2\}, \{1\}, \{2\}, \{1\}, \{2\}, \{1\}, \{2\}, \{1\}, \{2\}, \{1\}, \{2\}, \{2\}, \{1\}, \{2\}, \{2\}, \{2\}, \{1\}, \{2\}, \{2\}, \{2\}, \{2\}, \{2\}, \{2\}, \{2\}, \{2$
<pre>While[Length[sstr] > 0, ee = sstr[[1]];</pre>	(VA. 1. VD.). (3). (VE. 0. VB.). (3).
<pre>sstr = Drop[sstr, 1]; ss = Join[ss, {ee, NextShiftCanBe[ee, ss[-1]][1]}];</pre>	
<pre>SS) // (xx = Drop[AdjustEdges[yy = #], -1]) & // CleanoutHilbertTempString</pre>	$\{vC_2, 0, vD_1\}, \{1\}, \{vA_2, 0, vB_2\}, \{2\}, \{2\}, \{vB_2\}, \{vB$
<pre>RandomSubstitution[str_] := (ss = RandomChoice[{H} &/@ {vA1, vB1, vC1, vD1, vA2, vB2, vC2, vD2, vE, vF}]; sstr = str:</pre>	$\{vD_1, 0, vC_1\}, \{1\}, \{vC_1, 1, vC_2\}, \{0\},\$
<pre>While[Length[sstr] > 0,</pre>	(VE 3 VA.) (0) (VE 1 VC.) (2)
sstr = Drop[sstr, 1];	
ss = Join[ss, (ee, Kandomenoice[kextshirtCanbe[ee, ss[-1]]])]); ss	$\{vA_1, 0, vB_2\}, \{2\}, \{vE, 0, vB_2\}, \{3\},$
) // (xx = Drop(AdjustEdges(yy = #], -1]) & // CleanoutHilbertTempString	
(*these are our starting strings*) sstr = str;	$\{VC_1, 0, VD_1\}, \{1\}, \{VA_2, 0, VB_1\}, \{1\},$
While[Length[sstr] > 0, ee = sstr[[1]];	$\{vF, 0, vE\}, \{3\}, \{vA_1, 0, vB_1\}, \{3\},$
sstr = Drop[sstr, 1]; ss = Join @@ (Join @@ (Outer[Append, (#[[1]]), #[[2]], 1] & /@	
({Append[#, ee], NextShiftCanBe[ee, #[[-1]]]} & /@ss)))];	$\{vC_2, 0, vE\}, \{1\}, \{vD_2, 0, vC_2\}, \{2\}, $
CanonicalSubstitution[str_] := ((ma 0 ma) (2) (ma 2 ma) (0)
ss = {vx1}; sstr = str;	$\{v_{A_2}, v_i, v_{F_j}, \{z_j, \{v_{A_1}, j, v_{A_1}\}, \{v_j\}, \}$
While[Length[sstr] > 0, ee = sstr[[1]];	$\{vF, 1, vC_2\}, \{0\}, \{vD_2, 3, vD_1\}\}$
<pre>sstr = Drop[sstr, 1]; ss = Join[ss, {ee, NextShiftCanBe[ee, ss[-1]][1]]];</pre>	
$\frac{33}{1 / (x_{x} = \text{Dron[AdjustEdges[y_{y} = 1]]} + 1 / CleanoutEilbertTemnString}$	
<pre>, /, (n = org(s) = subject[] = (sa = RandomChoice[[H] & /⊕ (vA₁, vB₁, vC₁, vD₁, vA₂, vB₂, vC₂, vD₂, vE, vF)]; satr = str;</pre>	
<pre>While[Length[sstr] > 0, ee = sstr[[1]]:</pre>	
<pre>sstr = Drop[sstr, 1];</pre>	These are the individual bricks themselves

sst = Drop[sstr, 1]; ss = Join[ss, (ee, RandomChoice[NextShiftCanBe[ee, ss[-1]]]]]; ss) // (xx = Drop[AdjustEdges[yy = #], -1]) & // CleanoutHilbertTempString These are the individual bricks themselves, and code to enumerate them.







... leading to this speciman, one of N possibilities.

Chaim sent Eugene the following message:



Each digit encoded a turn from one module to the next: 0 for none, 1 for a quarter turn, 2 for a half turn and 3 for a quarter turn the other way.

Eugene made special jigs, one for each digit, so the seams could be smoothly welded.

All together, each block of fifteen digits encoded a brick made up of sixteen modules.







Thurman Thomas and Lee Koehn.



There were thirty-two bricks, each with a unique place in the sculpture.

> The individual pieces weren't very uniform—next time we will use artistgrade plumbing.









As always, assembling the piece at the party is the best part of all.



Unfortunately, we'd left our carefully prepared notes back in the hotel and had to work out how to put it together again!









